PAT 463/563 (Fall 2025)

Music & Al

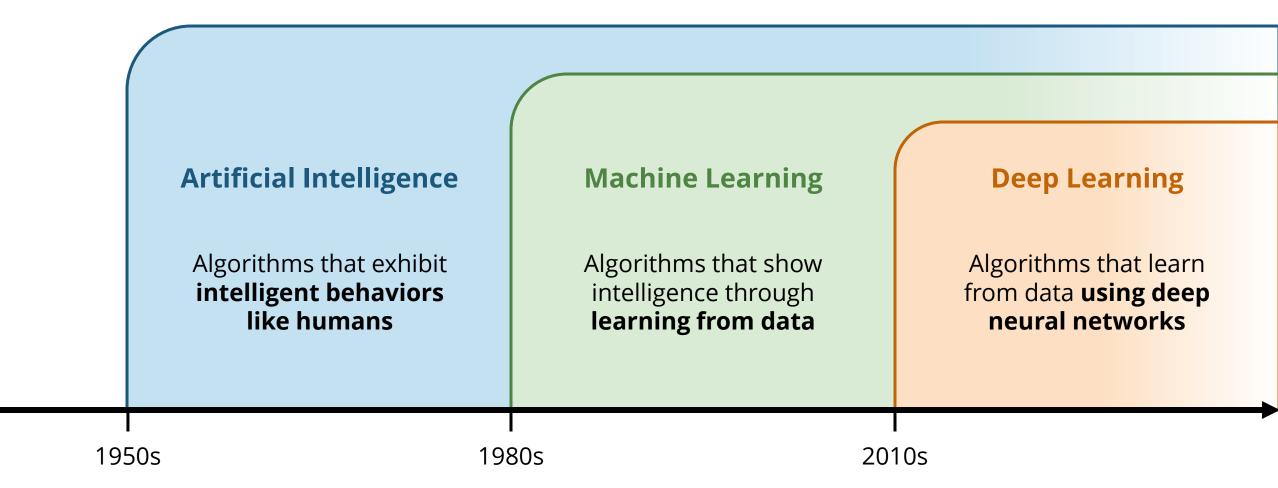
Lecture 6: Deep Learning Fundamentals

Instructor: Hao-Wen Dong



What is Deep Learning?

Al vs ML vs DL



Components of a Machine Learning Model

Optimization

Defining inputs & outputs

Improve on task T,

with respect to performance metric P,

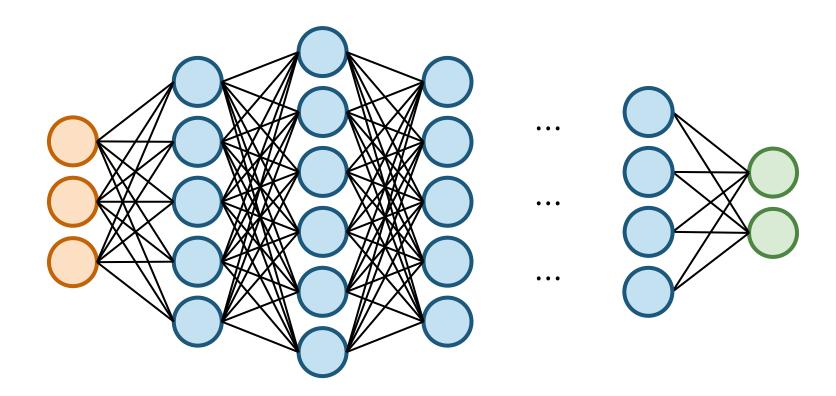
based on experience E

Objective function (loss function)

Training data

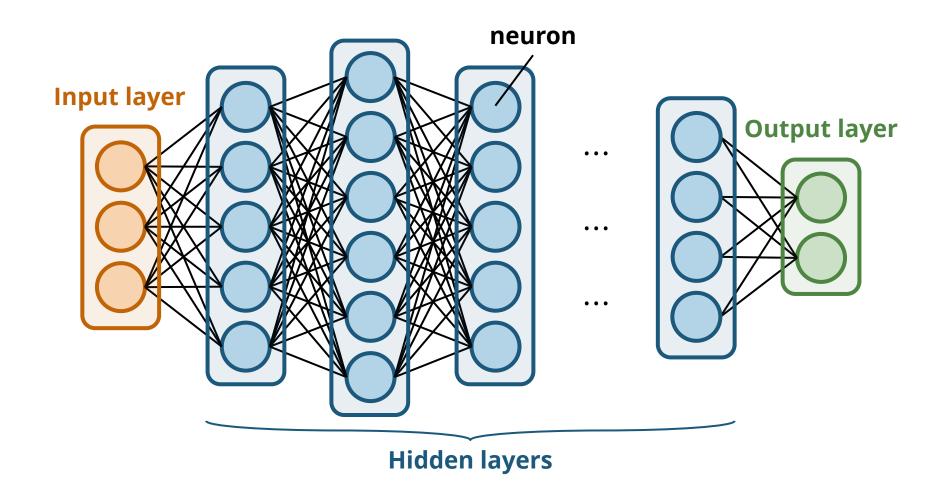
What is Deep Learning?

A type of machine learning that uses deep neural networks



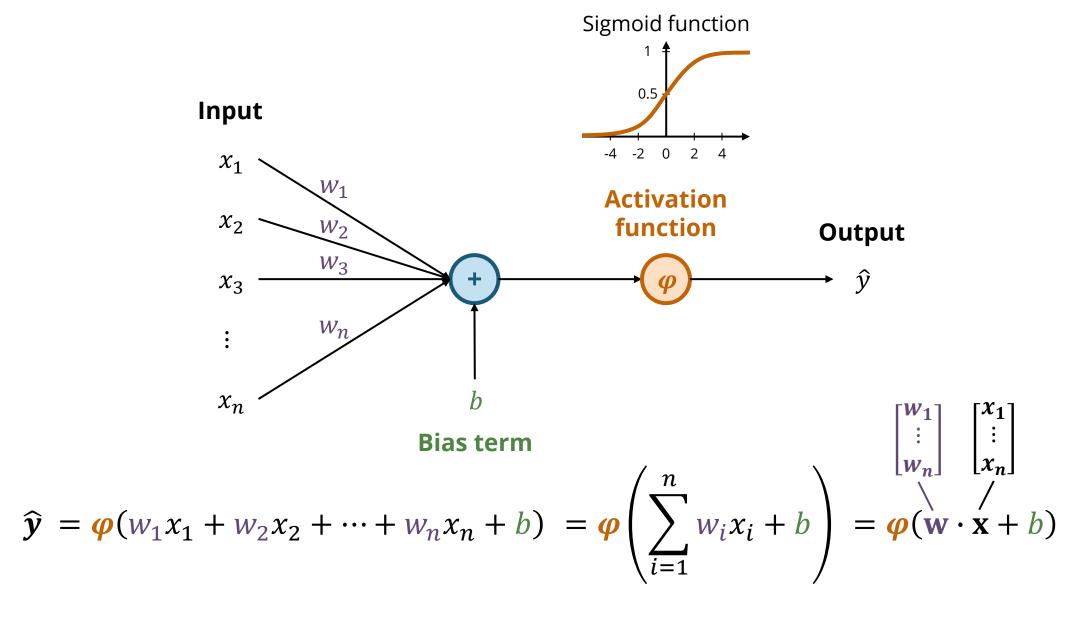
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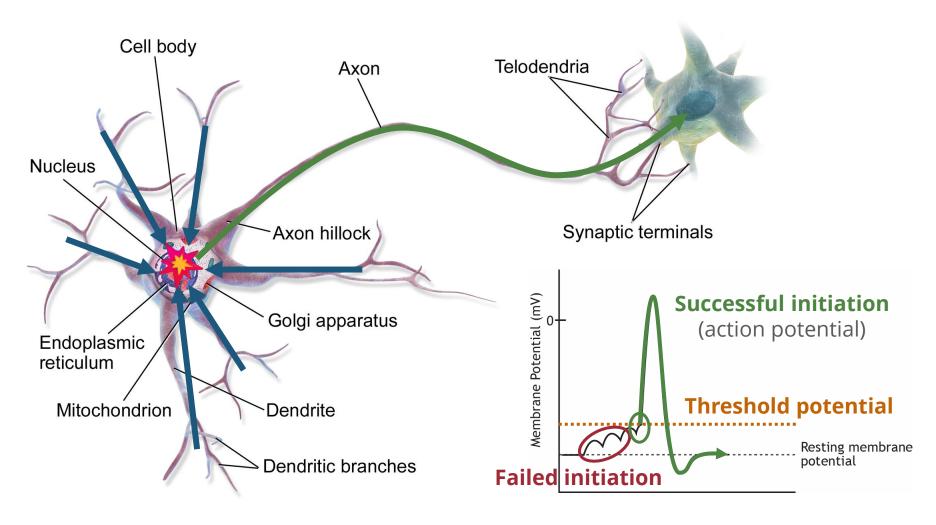


Neural Networks

Inside a Neuron



Human Neuron

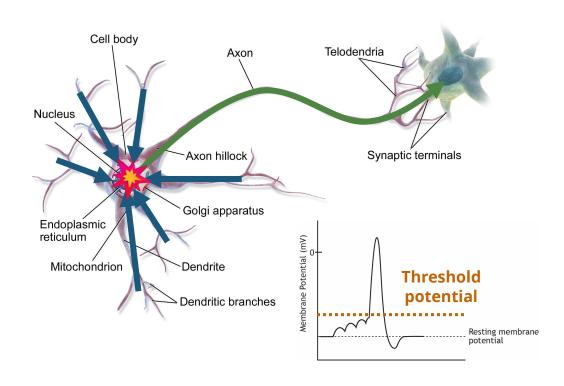


Artificial vs Human Neuron

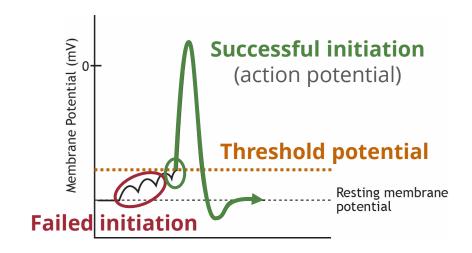
Artificial neuron

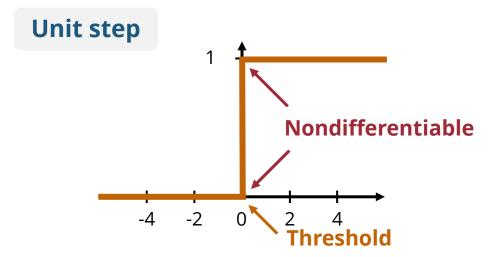
x_1 w_1 x_2 w_2 x_3 w_3 + φ \hat{y} \vdots w_n \vdots w_n b Sigmoid

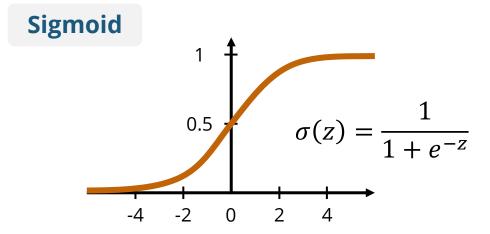
Human neuron



Why Sigmoid?







Why Bias Term?

Allow nonzero outputs when all inputs are zero

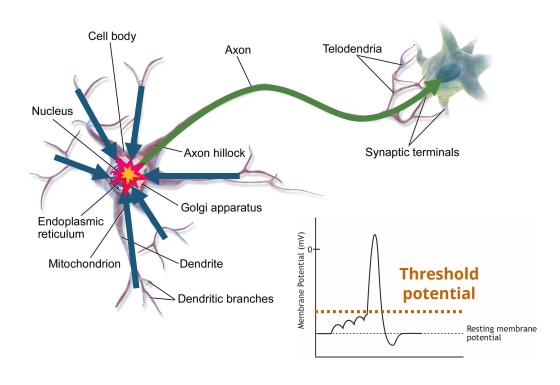
$$\hat{y} = \varphi(w_1 x_1^0 + w_2 x_2^0 + \dots + w_n x_n^0 + b) = \varphi(b)$$

Artificial vs Human Neuron

Artificial neuron

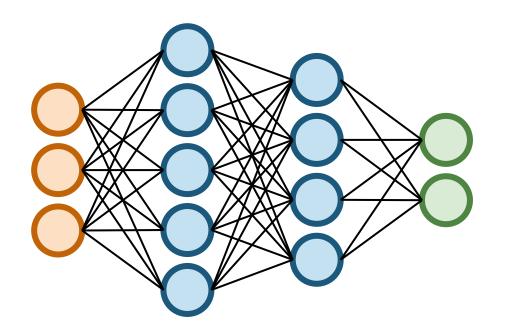
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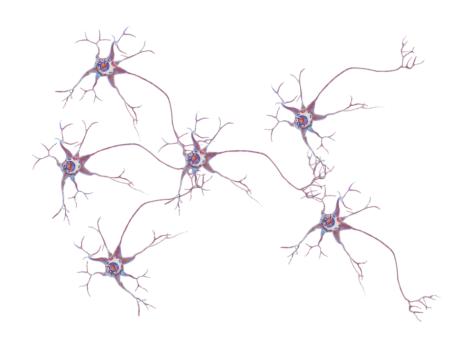
Human neuron



Artificial Neural Networks

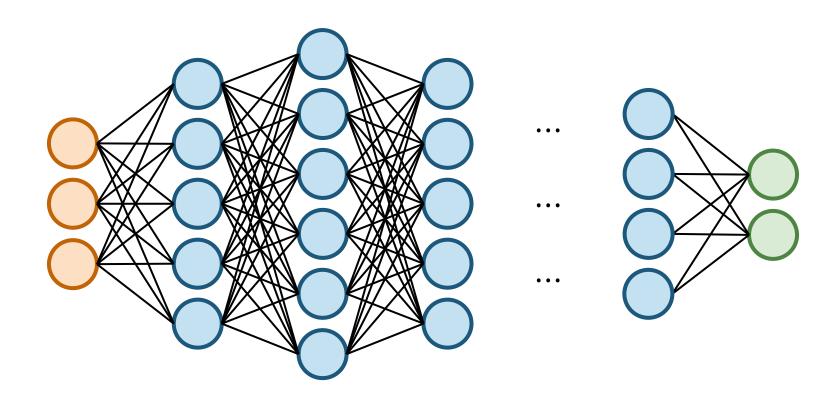
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 - Lacking functional hierarchy, high-level feedback loops, memory module, etc.
 - Human brains work more like spiking neural networks → Efficiency!

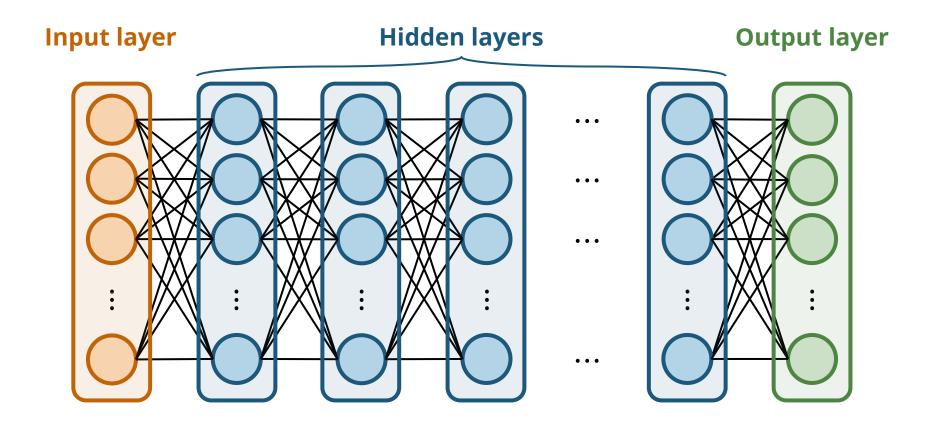


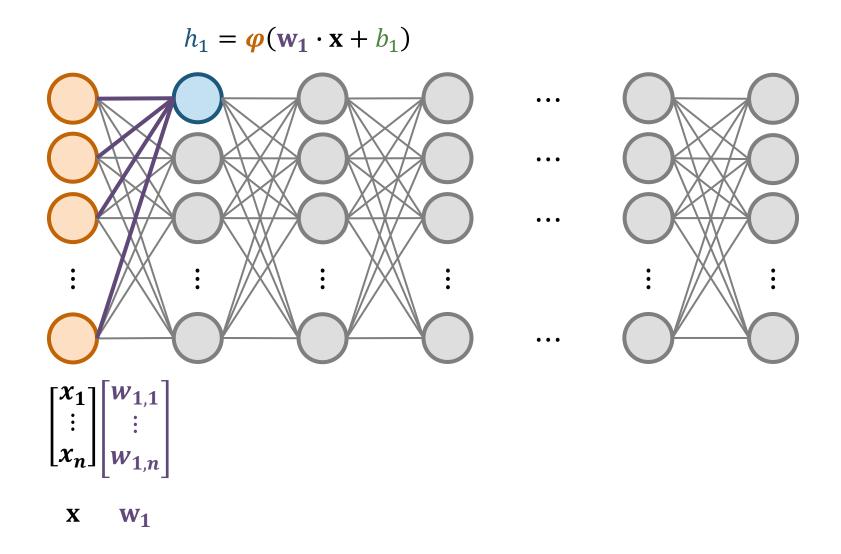


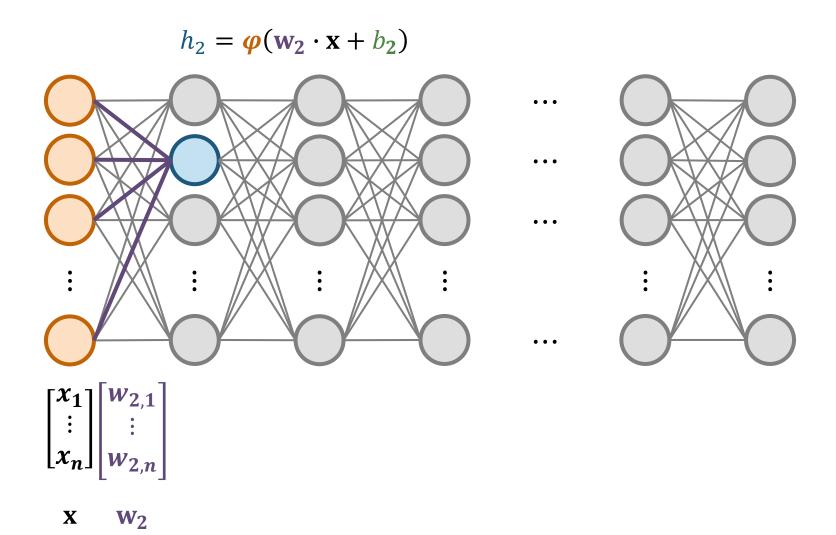
Fully Connected Feedforward Network

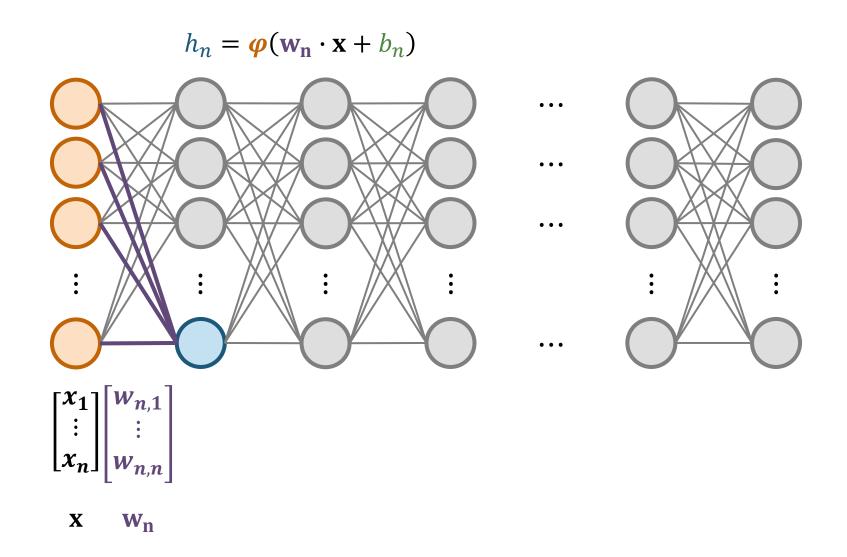
Most basic form of deep neural networks

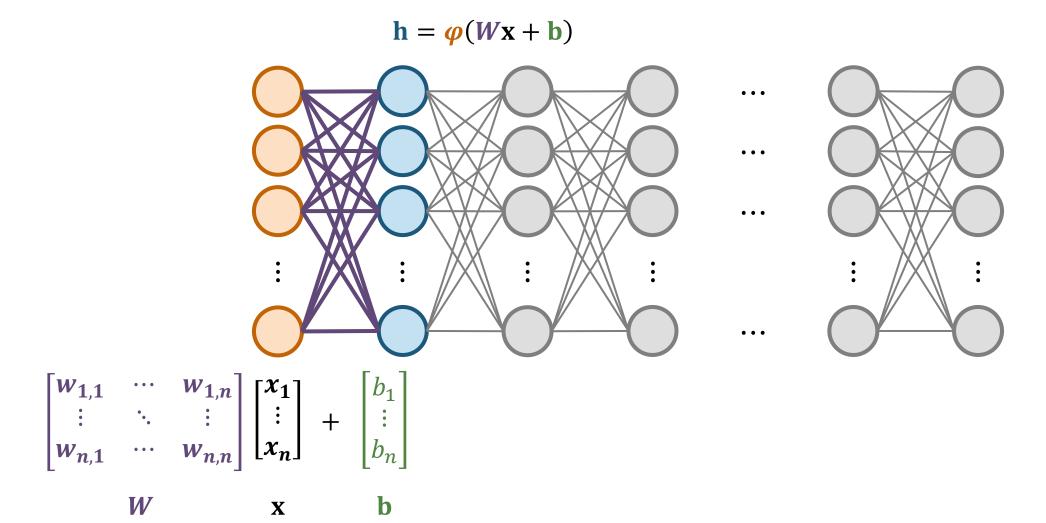


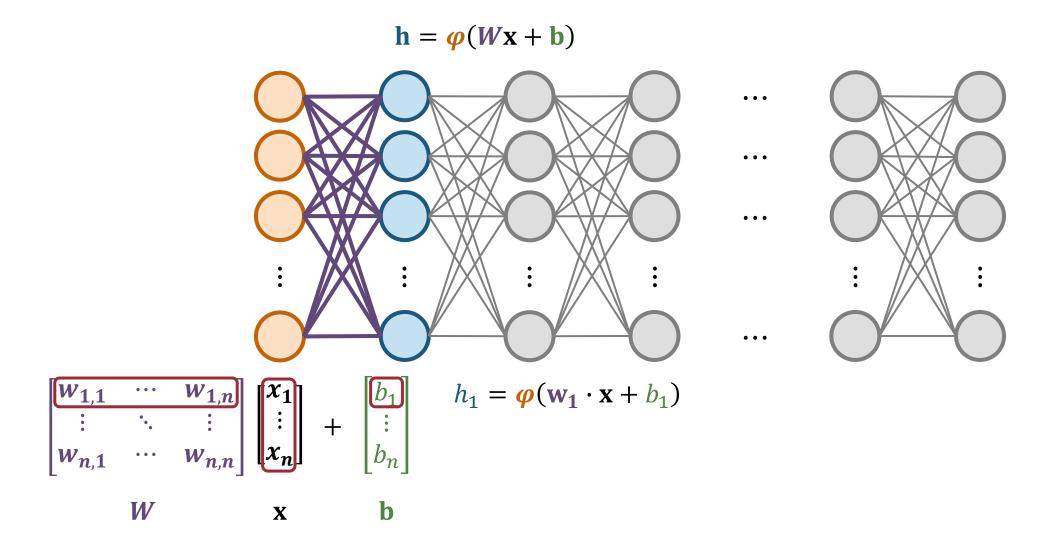


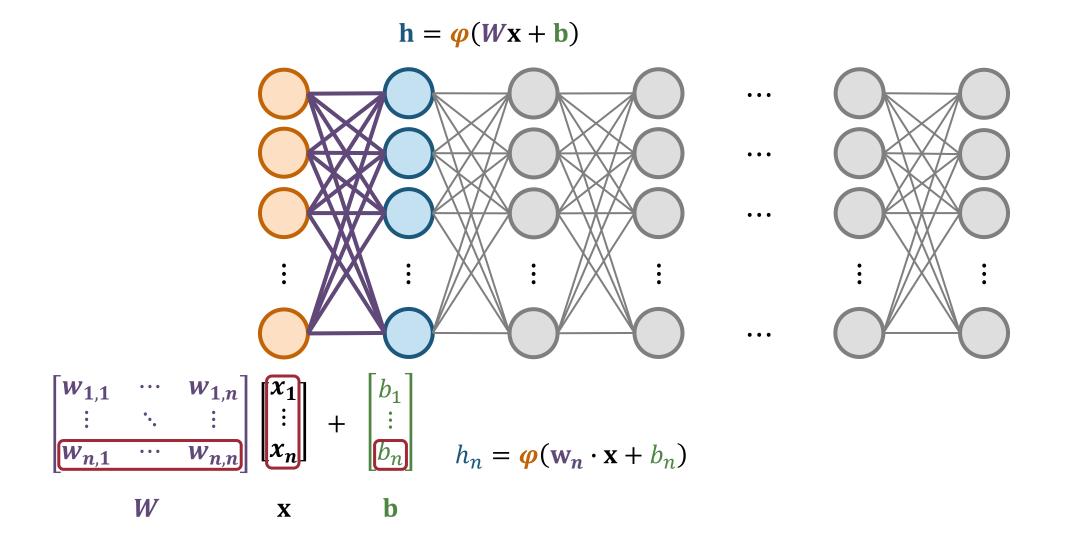


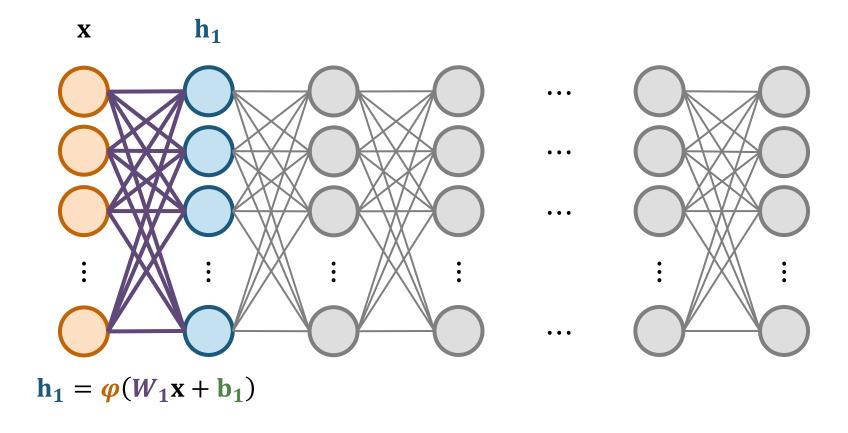


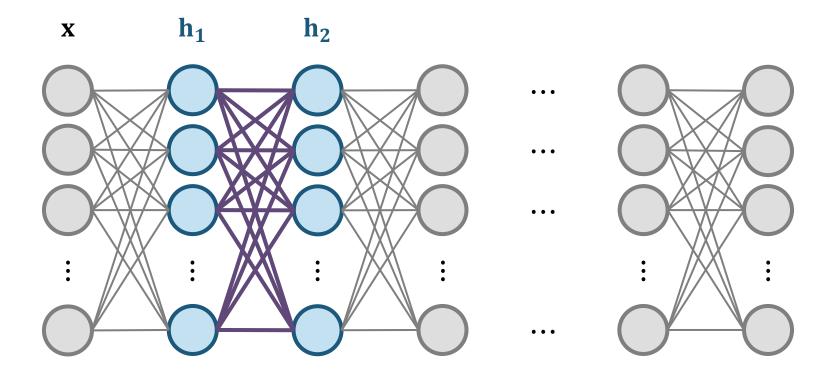




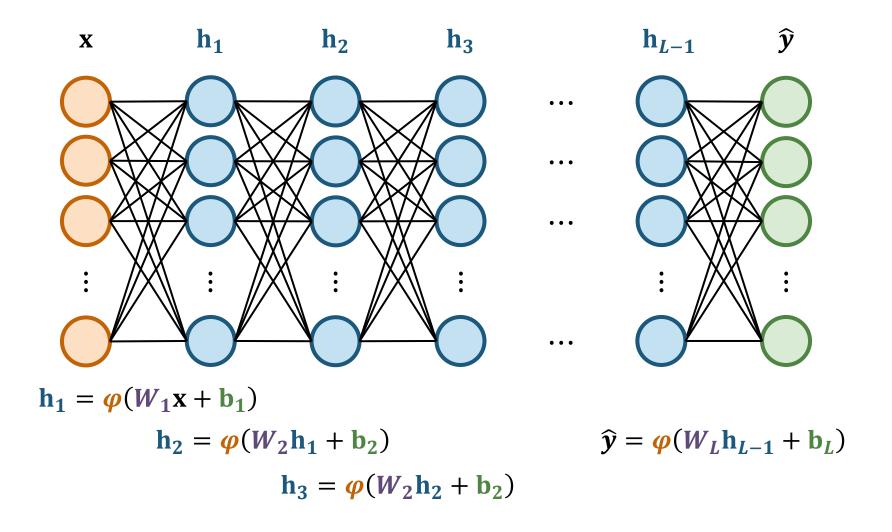




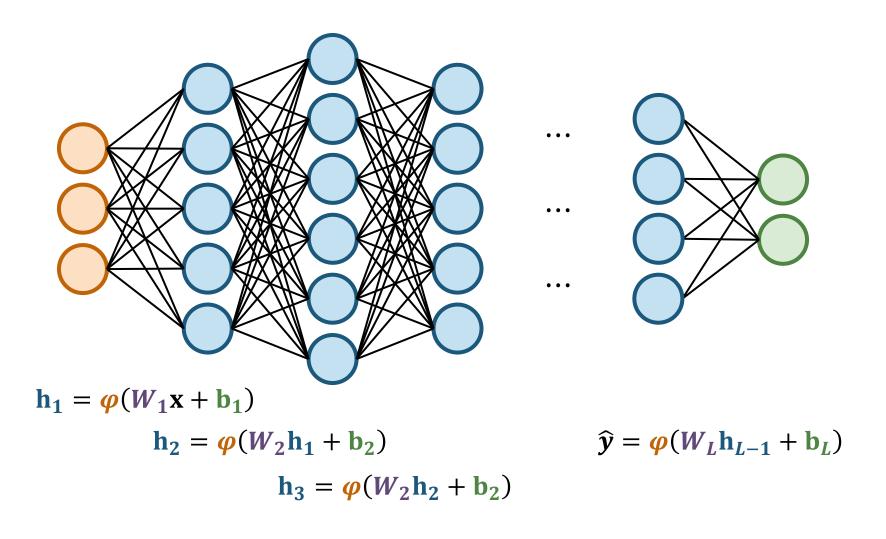




$$\mathbf{h}_2 = \boldsymbol{\varphi}(W_2\mathbf{h}_1 + \mathbf{b}_2)$$

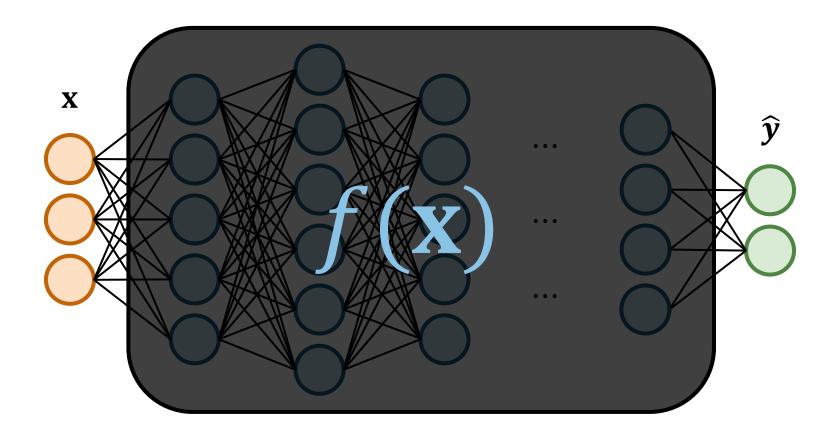


Fully Connected Feedforward Network



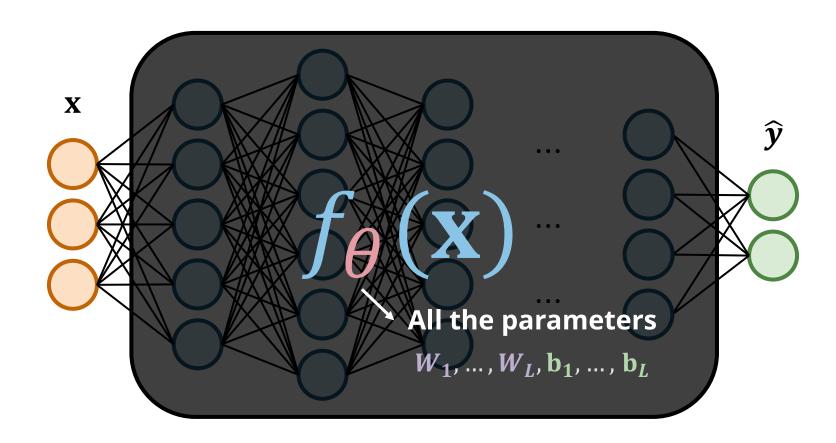
Neural Networks are Parameterized Functions

A neural network represents a set of functions

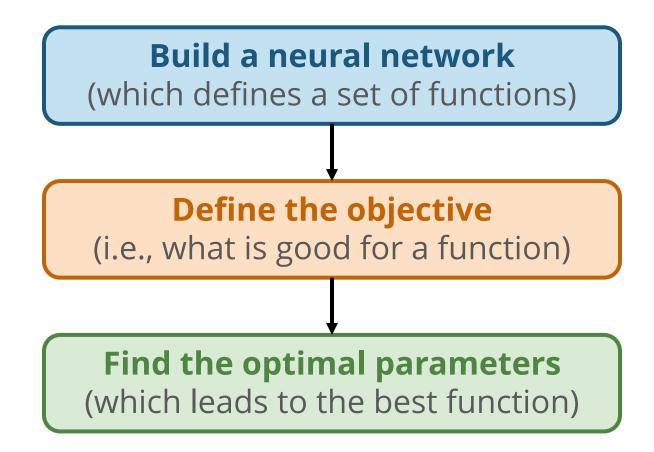


Neural Networks are Parameterized Functions

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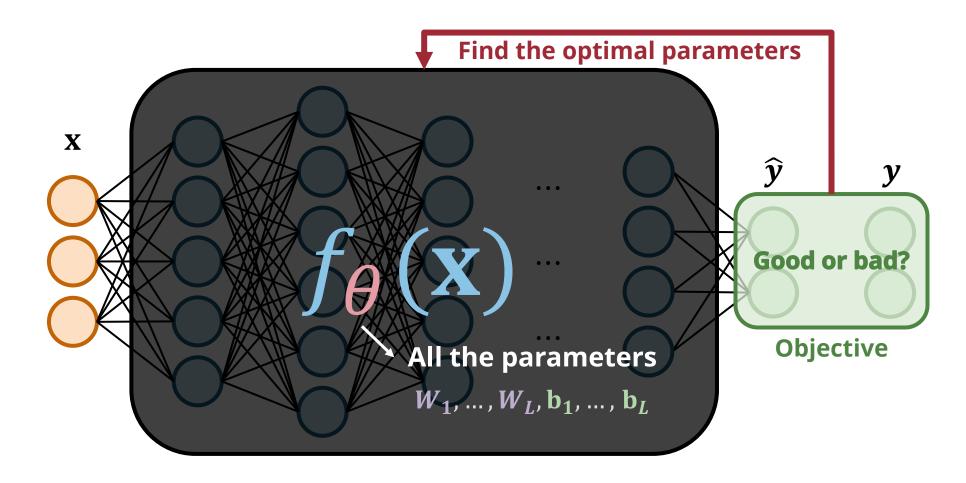


Training a Neural Network



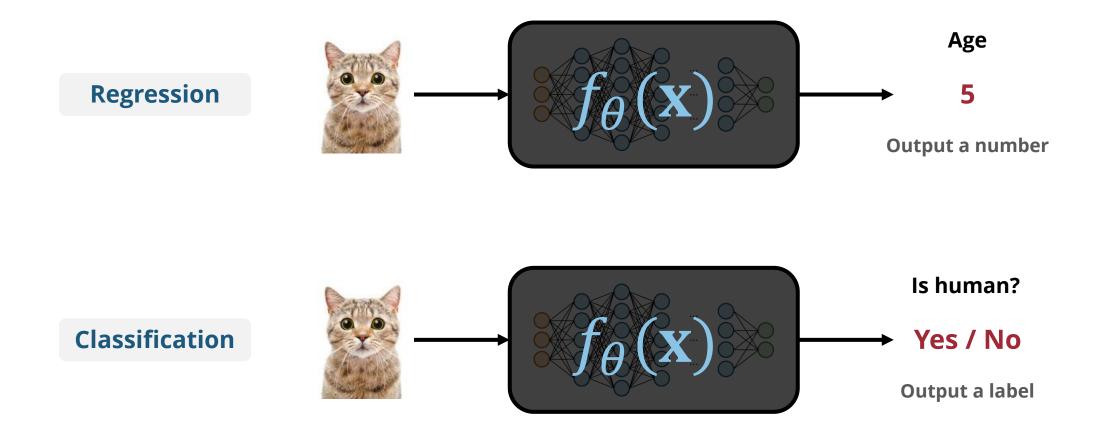
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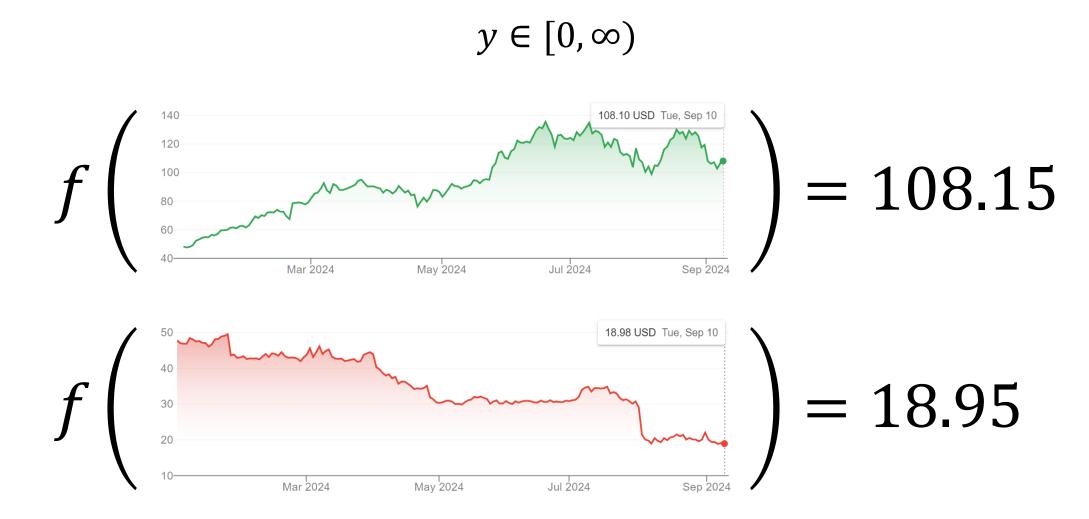


Regression vs Classification

Regression vs Classification



Regression Example: Stock Price Prediction



Regression Example: Depth Estimation

$$\mathbf{y} \in [0, \infty)^{W \times H}$$

Classification Example: Image Recognition

 $y \in \{\text{cat, dog, bear, bird}\}\$

$$y \in \{0, 1, 2, \dots, 9\}$$

$$f()) = cat$$

$$f(\mathcal{V}) = dog$$

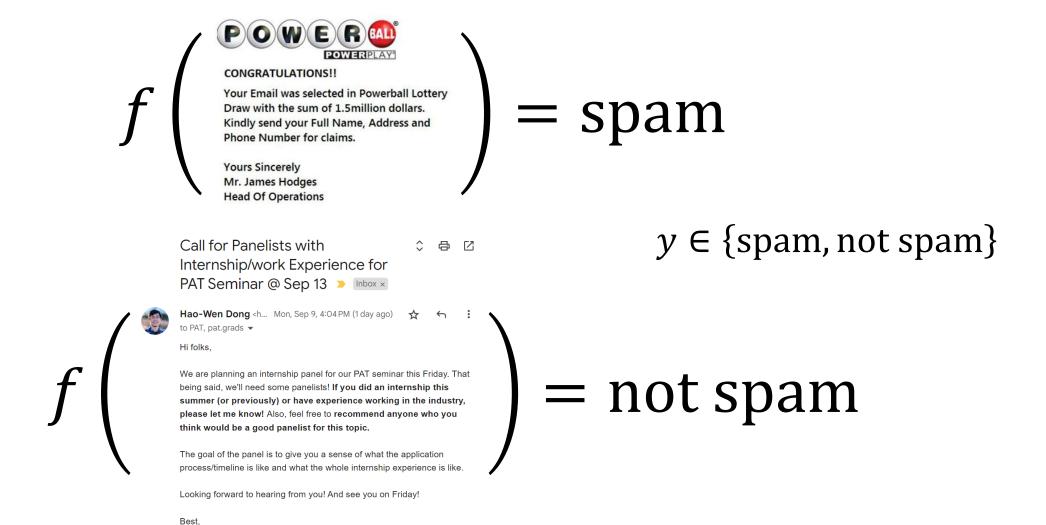
$$f(M) = bear$$

$$f(8) = 8$$

$$f(6) = 6$$

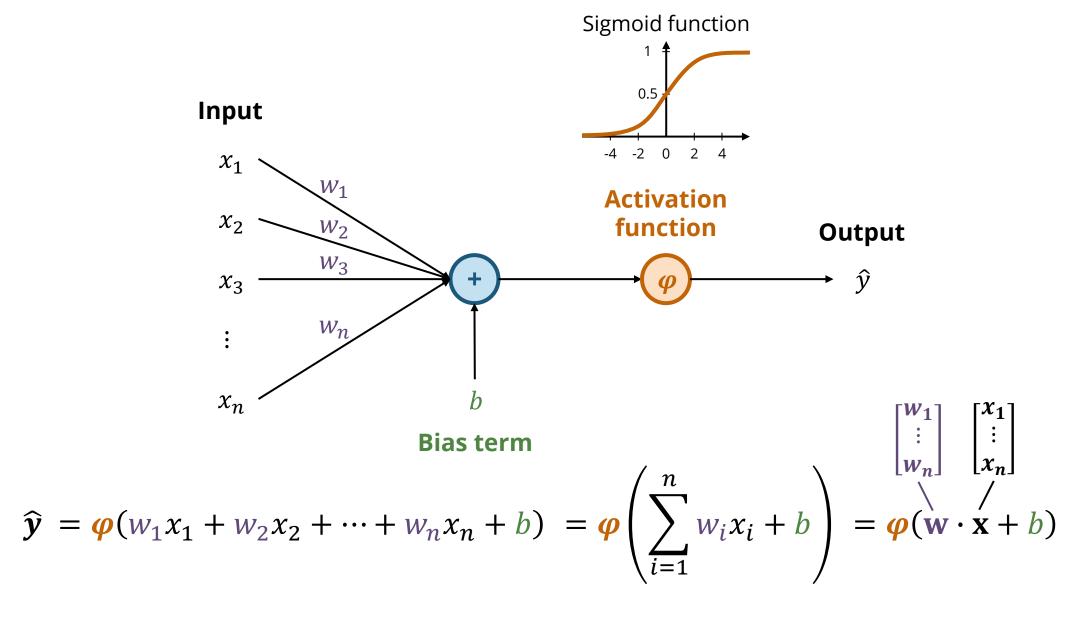
Classification Example: Spam Filter

Herman



Activation Functions

Inside a Neuron

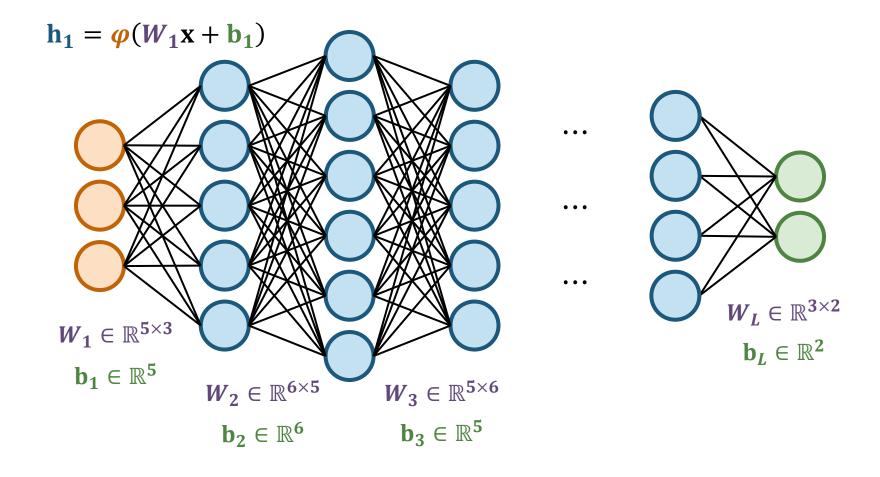


- Activation functions introduce nonlinearity to a neural network
- A linear function is a weighted sum of the inputs (plus a bias term)

$$f(x_1, x_2, ..., x_n) = a_1x_1 + a_2x_2 + a_3x_3 + ... + a_nx_n + b$$

- Examples of nonlinear functions:
 - $\cdot f(x_1) = \frac{1}{x_1}$
 - $f(x_1) = x_1^2$
 - $f(x_1) = e^x$
 - $f(x_1, x_2) = x_1 x_2$

Nonlinear functions are hard to model and approximate. That's where deep neural networks shine!



$$\hat{y} = \varphi(W_{L}h_{L-1} + b_{L})$$

$$\hat{y} = \varphi(W_{L}h_{L-1} + b_{L})$$

$$\hat{y} = \varphi(W_{L}h_{L-2} + b_{L-1}) + b_{L})$$

$$h_{3} = \varphi(W_{3}h_{2} + b_{3})$$

$$\hat{y} = \varphi(W_{L}\varphi(W_{L-1}h_{L-2} + b_{L-1}) + b_{L})$$

$$\vdots$$

$$\vdots$$

$$\hat{y} = \varphi(W_{L}h_{L-1} + b_{L})$$

$$\hat{y} = \varphi(W_{L}\varphi(W_{L-1}\varphi(W_{L-2}h_{L-3} + b_{L-2}) + b_{L-1}) + b_{L})$$

$$\vdots$$

With activation functions, a neural network can represent nonlinear functions

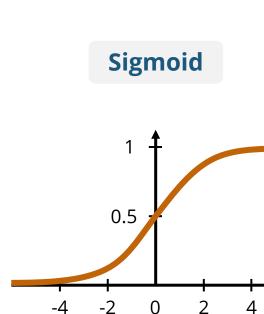
$$\widehat{\mathbf{y}} = \boldsymbol{\varphi}(W_L \ \boldsymbol{\varphi}(W_{L-1} \ \boldsymbol{\varphi}(W_{L-2} \ \boldsymbol{\varphi}(\cdots \mathbf{x} \cdots) + \mathbf{b}_{L-2}) + \mathbf{b}_{L-1}) + \mathbf{b}_L)$$



$$\hat{y} = W_L(W_{L-1}(W_{L-2}(\cdots x \cdots) + b_{L-2}) + b_{L-1}) + b_L$$

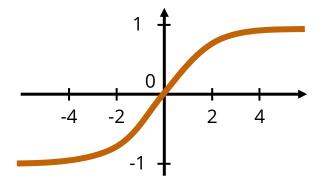
Without activation functions, a neural network can only represent linear functions

Commonly Used Activation Functions



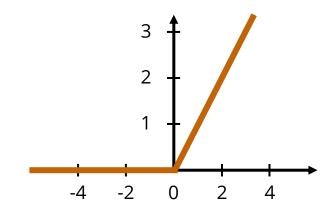
$$\sigma(z) = \frac{1}{1 + e^{-z}}$$

tanh



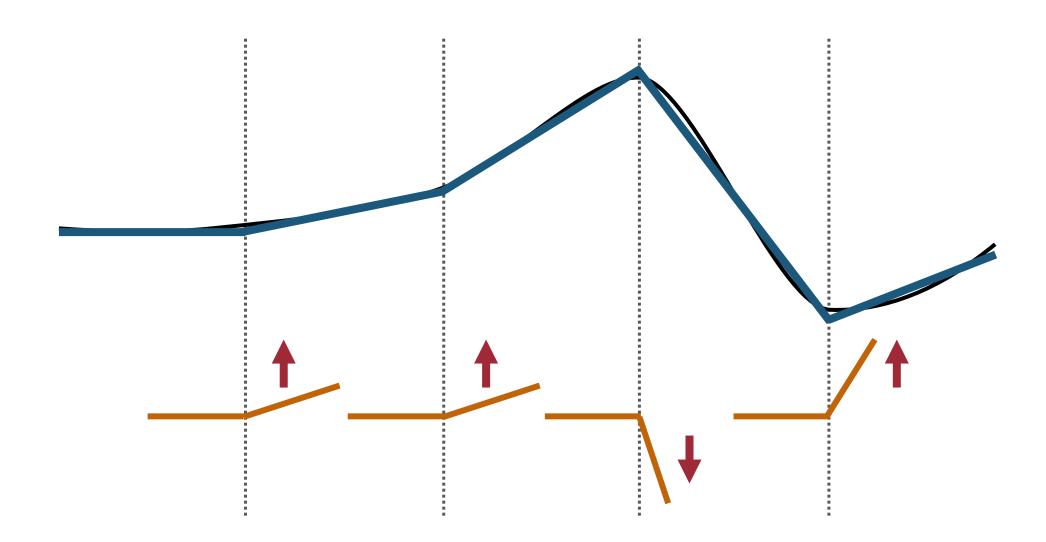
$$\tanh(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$

ReLU



$$ReLU(z) = \begin{cases} z, & \text{if } z \ge 0 \\ 0, & \text{otherwise} \end{cases}$$

ReLUs & Piecewise Linear Functions

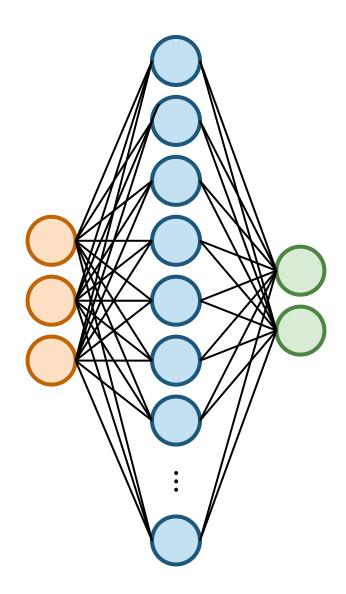


Expressiveness of Neural Networks

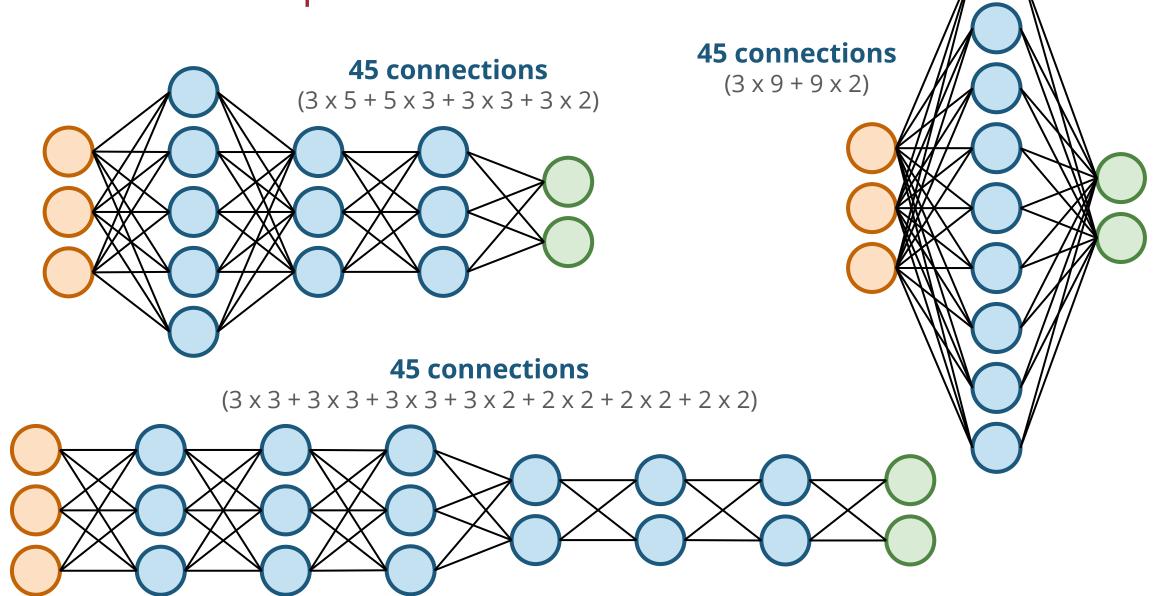
Universal Approximation Theorem

- A neural network with one hidden layer can approximate any continuous function given sufficient hidden neurons and appropriate activation functions
 - Sigmoid, ReLUs are good activation functions

Then why do we want to go deep?



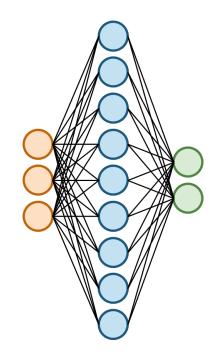
Shallow vs Deep Neural Networks



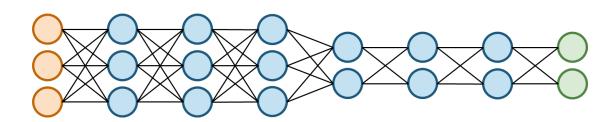
Shallow vs Deep Neural Networks – In Practice

Shallow neural nets

Deep neural nets



Less expressive (less parameter efficient)



More expressive

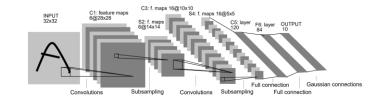
(more parameter efficient)

How Deep is Deep Enough?

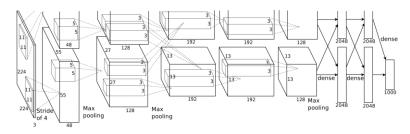
Deeper is not always better

- Actual number of parameters
- Optimization difficulties
- Data size
- Inductive bias of the model

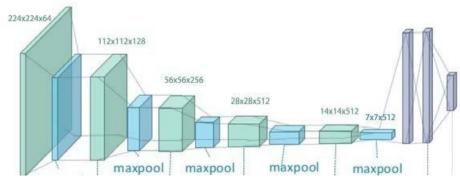




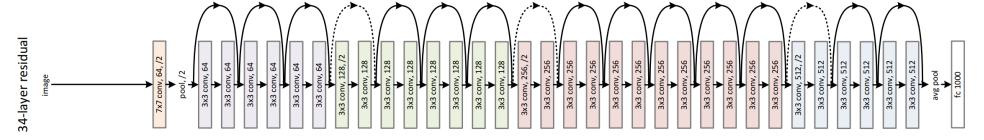
AlexNet (2012)



VGG-19 (2015)

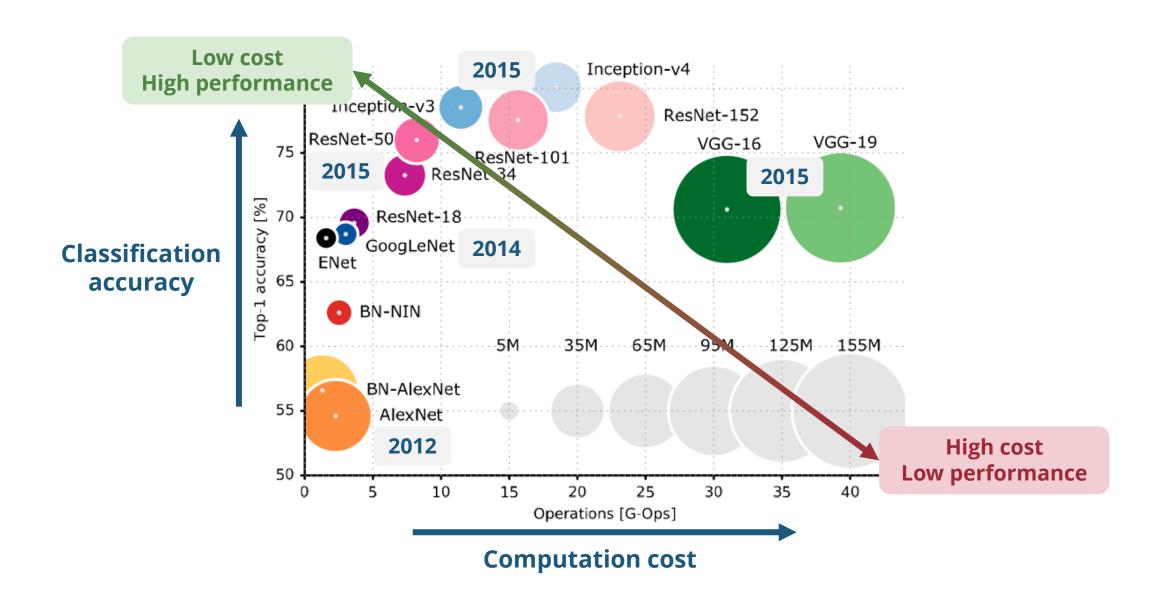


ResNet (2015)



Yann LeCun, Léon Bottou, Yoshua Bengio, and Patrick Haffner, "Gradient-based learning applied to document recognition," Proc. IEEE, 1998. Alex Krizhevsky, Ilya Sutskever, and Geoffrey E. Hinton, "ImageNet Classification with Deep Convolutional Neural Networks," NeurIPS, 2012. Karen Simonyan and Andrew Zisserman, "Very Deep Convolutional Networks for Large-Scale Image Recognition," ICLR, 2015. Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun, "Deep Residual Learning for Image Recognition," CVPR, 2016.

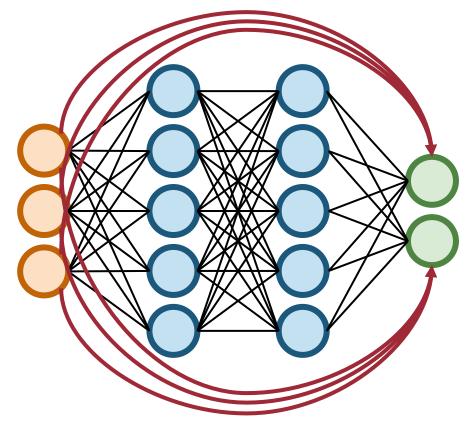
Computation Cost vs Classification Accuracy



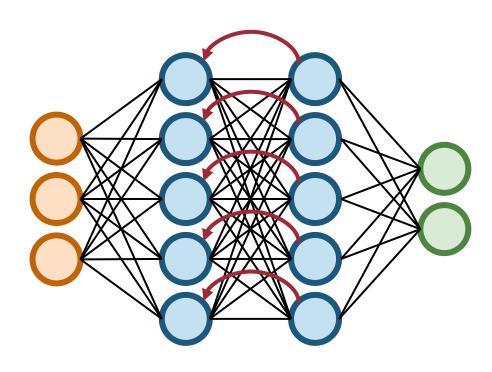
Neural Networks are NOT always Layer-by-Layer

Skip connections

Feedback loops







Used in RNNs, LSTMs, GRUs

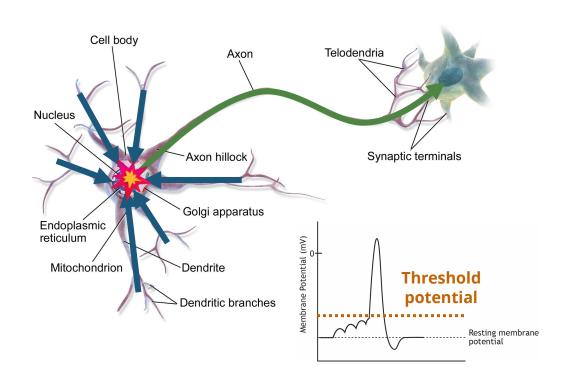
Recap

Artificial vs Human Neuron

Artificial neuron

x_1 w_1 x_2 w_2 x_3 w_3 + φ \hat{y} \vdots w_n b Sigmoid

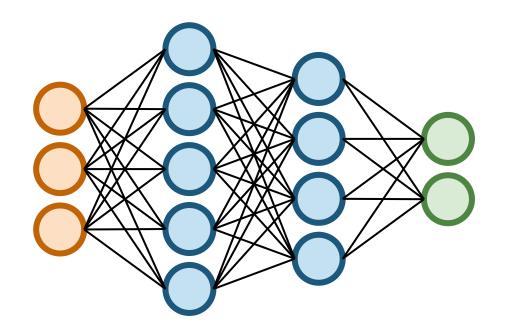
Human neuron

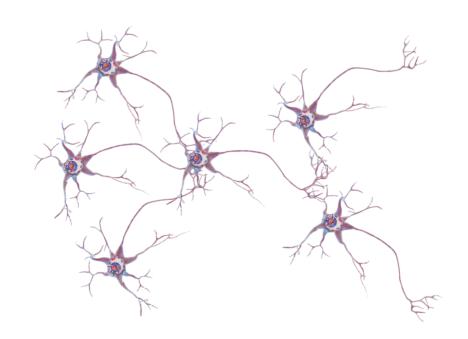


Casey Henley, Introduction to Neuroscience 54

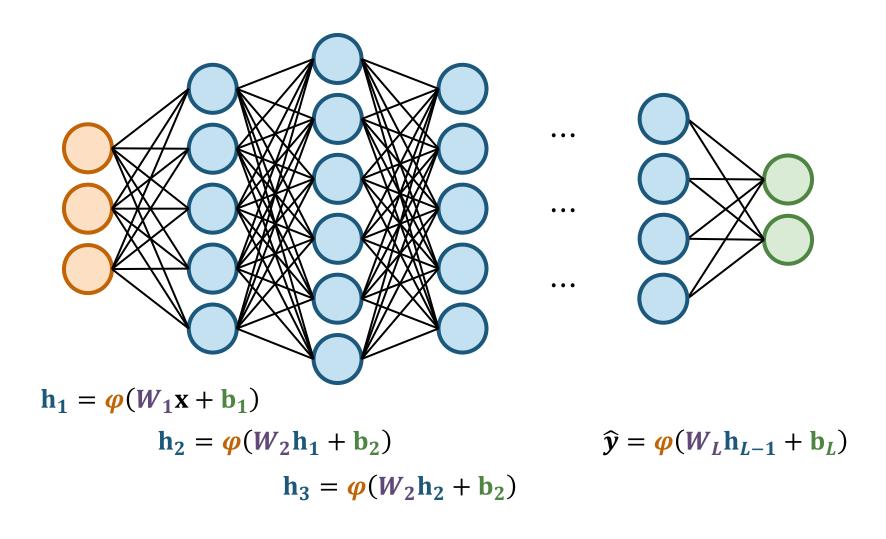
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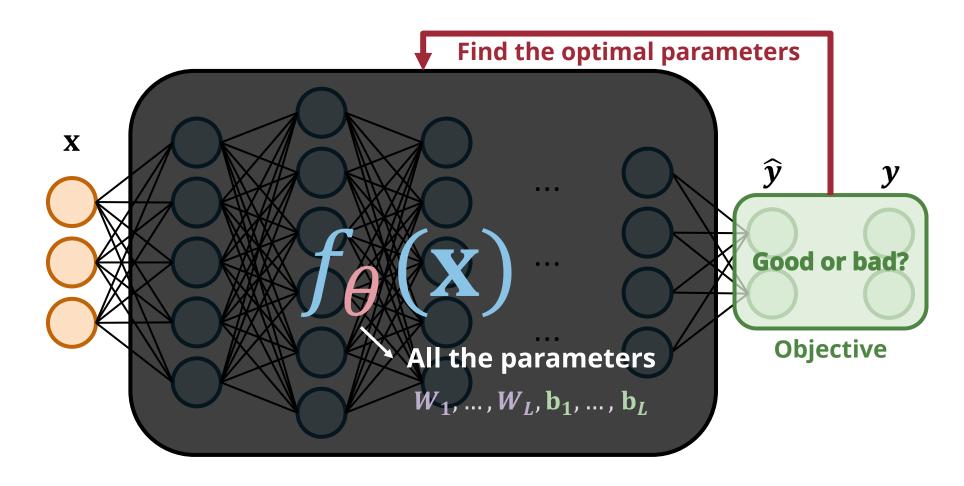


Fully Connected Feedforward Network

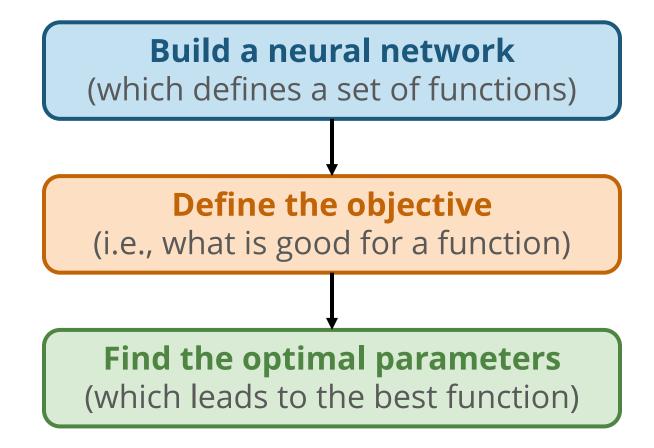


Neural Networks are Parameterized Functions

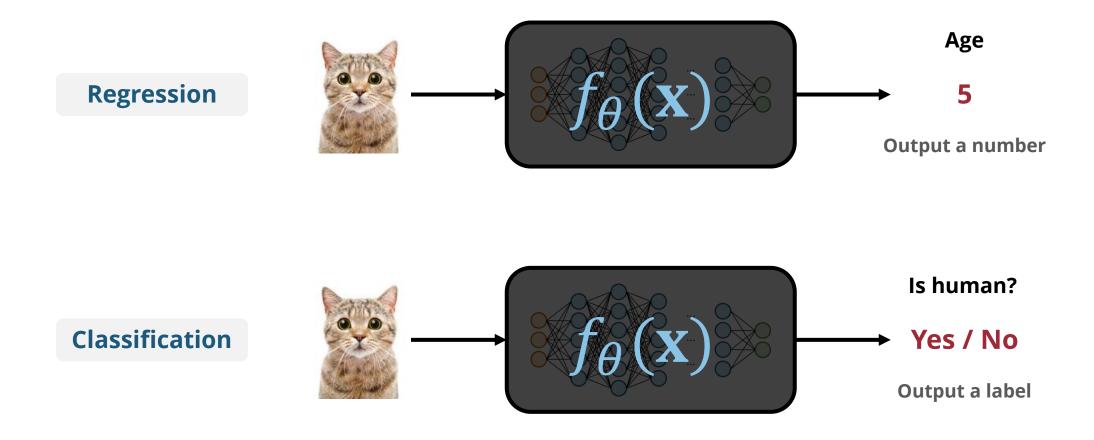
A neural network represents a set of functions



Training a Neural Network



Regression vs Classification



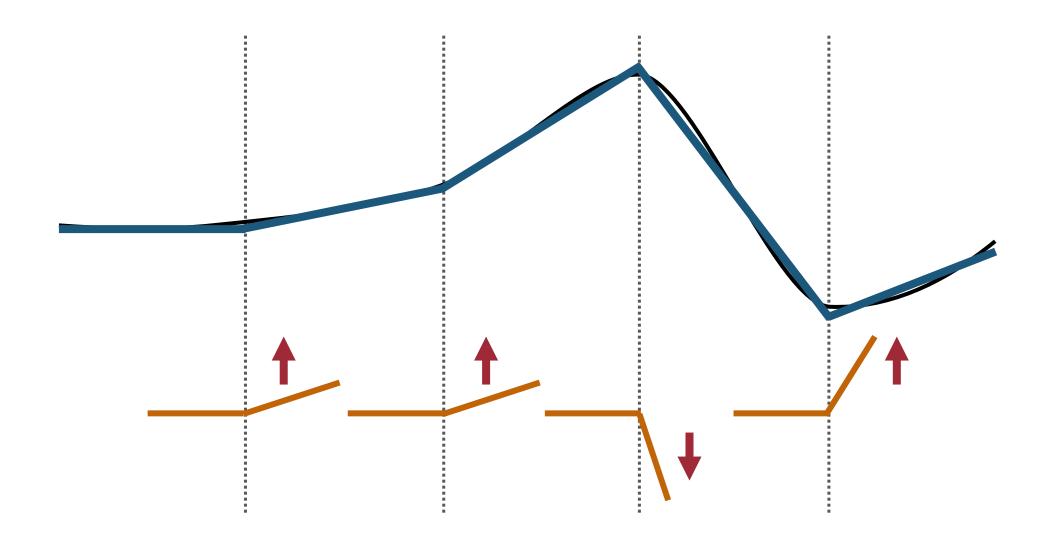
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Without activation functions, a neural network can only represent linear functions

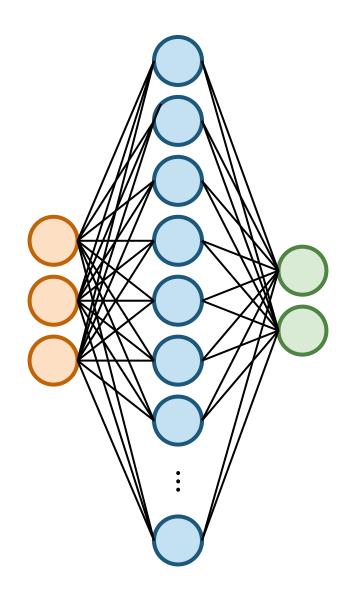
ReLUs & Piecewise Linear Functions



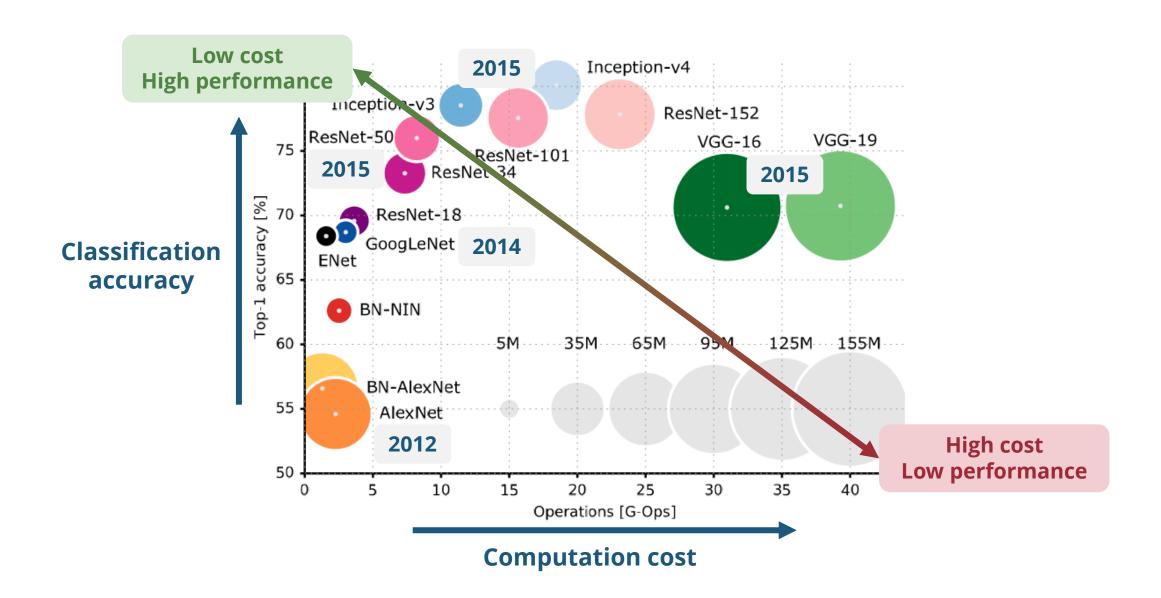
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Computation Cost vs Classification Accuracy



Next Lecture

Deep Learning Fundamentals II

